CS 4440 A Emerging Database **Technologies**

Lecture 3 01/13/25

Logistics

Office hour

- \circ Instructor: Wed 11:30-12:30 (starting next week)
- Jeff: Thur 1:30-2:30
- Tianji: Fri 10-11

Project proposal draft released

- Groups of 3-5, total of 16 groups
- Sign up under People->Project Groups on canvas
- Use the "Find teammates" post on Piazza
- Due Feb 3 (not graded, intended for feedback)

Reading Materials

Database Systems: The Complete Book (2nd edition)

• Chapter 3: Design Theory for Relational Databases $(3.1 - 3.3)$

Acknowledgement: The following slides have been adapted from EE477 (Database and Big Data Systems) taught by Steven Whang and CS145 (Intro to Big Data Systems) taught by Peter Bailis

Agenda

1. Normal forms & functional dependencies

2. Finding functional dependencies

3. Closures, superkeys & keys

1. Normal forms & functional dependencies

Normal Forms

- \bullet 1st Normal Form (1NF) = All tables are flat
- 2nd Normal Form = disused
- Boyce-Codd Normal Form (BCNF)
- 3rd Normal Form (3NF)
- \triangleq 4^{th} and 5^{th} Normal Forms = see textbooks

1 st Normal Form (1NF)

Violates 1NF.

In 1st NF

1NF Constraint: Types must be atomic!

Normal Forms

- \bullet 1st Normal Form (1NF) = All tables are flat
- 2nd Normal Form = disused
- **Boyce-Codd Normal Form (BCNF)**
- 3rd Normal Form (3NF)

DB designs based on functional dependencies, intended to prevent data anomalies

Our focus in this lecture + next one

 \triangleq 4^{th} and 5^{th} Normal Forms = see textbooks

A poorly designed database causes *anomalies*:

If every course is in only one room, contains **redundant** information!

A poorly designed database causes *anomalies*:

If we update the room number for one tuple, we get inconsistent $data = an update$ **anomaly**

A poorly designed database causes *anomalies*:

If everyone drops the class, we lose what room the class is in! = a delete anomaly

A poorly designed database causes *anomalies*:

Similarly, we can't reserve a room without students = an **insert anomaly**

Eliminate anomalies by decomposing relations.

- Redundancy?
- Update anomaly?
- Delete anomaly?
- Insert anomaly?

Goal: develop theory to understand why this design may be better and how to find this decomposition…

Functional Dependencies

Functional dependency (FD)

Definition: if two tuples of R agree on all the attributes A_1 , A_2 , ..., A_n , they must also agree on (or functionally determine) B_1 , $\mathsf{B}_2,$..., B_{m}

• Denoted as $A_1A_2... A_n \rightarrow B_1B_2... B_m$

A->B means that "whenever two tuples agree on A then they agree on B."

Splitting/combining rule

• Splitting/combining can be applied to the **right sides** of FD's

Splitting/combining rule

● For example,

title year \rightarrow length genre studioName

Splitting rule

• Splitting rule does not apply to the left sides of FD's

title year \rightarrow length

title \rightarrow length $year \rightarrow length$

Functional Dependencies as Constraints

A functional dependency is a form of constraint

- Holds on some instances (but not others) – can check whether there are violations
- Part of the schema, helps define a valid instance

Recall: an instance of a schema is a multiset of tuples conforming to that schema, i.e. a table

Note: The FD ${ \text{Course} } > { \text{Room} }$ holds on this instance

Functional Dependencies as Constraints

Note that:

- You can check if an FD is violated by examining a single instance;
- However, you **cannot prove** that an FD is part of the schema by examining a single instance.
	- This would require checking every valid instance

However, cannot prove that the FD ${Course} \rightarrow {Room}$ is part of the schema

Trivial functional dependencies

A constraint is *trivial* if it holds for every possible instance of the relation.

Trivial FDs: $A_1A_2... A_n \rightarrow B_1 B_2... B_m$ such that ${B_1, B_2, \ldots B_m} \subseteq {A_1, A_2, \ldots, A_n}$

Trivial dependency rule: $A_1A_2... A_n \rightarrow B_1 B_2... B_m$ is equivalent to $A_1A_2... A_n \rightarrow C_1 C_2... C_k$, where the C's are the B's that are not also A's

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In-class Exercise

Q1: Find an FD that holds on this instance Q2: Find an FD that is violated on this instance

2. Finding functional dependencies

FDs for Relational Schema Design

High-level idea: why do we care about FDs?

- 1. Start with some relational schema
- 2. Find out its functional dependencies (FDs)

This part can be tricky!

- 3. Use these to design a better schema
	- 1. One which minimizes possibility of anomalies

Finding Functional Dependencies

There can be a large number of FDs…

Let's start with this problem:

Given a set of FDs, $F = \{f_1, \ldots f_n\}$, does an FD *g* hold?

Three simple rules called Armstrong's Rules.

- 1. Reflexivity,
- 2. Augmentation,
- 3. Transitivity

You can derive any FDs that follows from a given set using these axioms:

1. Reflexivity: If Y is a subset of X, then $X \rightarrow Y$

This means that a set of attributes always determines a subset of itself

2. Augmentation: If $X \rightarrow Y$, then $XZ \rightarrow YZ$ for any Z This means we can add the same attributes to both sides of a functional dependency.

3. Transitivity: If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$

This allows us to chain functional dependencies.

• Does $AB \rightarrow D$ follow from the FDs below?

1. $AB \rightarrow C$ (given) 2. BC \rightarrow AD (given)

Does $AB \rightarrow D$ follow from the FDs below?

- 1. $AB \rightarrow C$ (given) 2. BC \rightarrow AD (given)
- 3. $AB \rightarrow BC$ (Augmentation on 1)

Does $AB \rightarrow D$ follow from the FDs below?

- 1. $AB \rightarrow C$ (given)
- 2. BC \rightarrow AD (given)
- 3. $AB \rightarrow BC$ (Augmentation on 1)
- 4. $AB \rightarrow AD$ (Transitivity on 2,3)

Does $AB \rightarrow D$ follow from the FDs below?

- 1. $AB \rightarrow C$ (given)
- 2. BC \rightarrow AD (given)
- 3. $AB \rightarrow BC$ (Augmentation on 1)
- 4. $AB \rightarrow AD$ (Transitivity on 2,3)
- 5. $AD \rightarrow D$ (Reflexivity)

Does $AB \rightarrow D$ follow from the FDs below?

- 1. AB \rightarrow C (given)
- 2. BC \rightarrow AD (given)
- 3. $AB \rightarrow BC$ (Augmentation on 1)
- 4. $AB \rightarrow AD$ (Transitivity on 2,3)
- 5. $AD \rightarrow D$ (Reflexivity)
- 6. AB \rightarrow D (Transitivity on 4,5)

Can we find an algorithmic way to do this?

Closures

$$
\begin{array}{c}\n\left\{\mathsf{A}, \mathsf{B}\right\}^{+} \\
\hline\n\mathsf{B}\mathsf{C} \rightarrow \mathsf{A}\mathsf{D} \\
\mathsf{D} \rightarrow \mathsf{E} \\
\mathsf{C}\mathsf{F} \rightarrow \mathsf{B}\n\end{array}\n\qquad\n\begin{array}{c}\n\{\mathsf{A}, \mathsf{B}\}^{+} \\
\hline\n\mathsf{A}, \mathsf{B}, \mathsf{C}, \mathsf{D}, \mathsf{E} \\
\hline\n\mathsf{A}, \mathsf{B}, \mathsf{C}, \mathsf{D}, \mathsf{E} \\
\hline\n\end{array}
$$

Given a set of attributes A_1, \ldots, A_n and a set of FDs F, the closure, $\{A_1, ..., A_n\}^+$ is the set of attributes B where ${A_1, ..., A_n} \rightarrow B$ follows from the FDs in F

$$
\begin{array}{c}\n\begin{array}{c}\n\{A, B\}^+ \\
\text{BC} \rightarrow \text{AD} \\
D \rightarrow \text{E} \\
\text{CF} \rightarrow \text{B}\n\end{array}\n\end{array}\n\qquad\n\begin{array}{c}\n\{A, B\}^+ \\
\text{A, B, C, D, E} \\
\hline\n\end{array}
$$

Cannot be expanded further, so this is a closure

Closure algorithm

○ discovers all true FDs

3. Closures, Superkeys & Keys

Why Do We Need the Closure?

With closure we can find all FD's easily

To check if $X \rightarrow A$

- 1. Compute X⁺
- 2. Check if $A \in X$

Note here that X is a set of attributes, but A is a single attribute. Why does considering FDs of this form suffice?

Recall the split/combine rule: $X \rightarrow A_1, ..., X \rightarrow A_n$ implies $X \rightarrow \{A_1, \ldots, A_n\}$

Using Closure to Infer ALL FDs

Step 1: Compute X^+ , for every set of attributes X:

 ${A}^+ = {A}$ ${B}^+ = {B,D}$ ${C}^+ = {C}$ ${D^+} = {D}$ ${A,B}^+ = {A,B,C,D}$ ${A, C}^+ = {A, C}$ ${A, D}^+ = {A, B, C, D}$ ${A,B,C}^+ = {A,B,D}^+ = {A,C,D}^+ = {A,B,C,D} {B,C,D}^+ = {B,C,D}$ ${A, B, C, D}^+ = {A, B, C, D}$

 ${A,B} \rightarrow C$ ${A, D} \rightarrow B$ $\{B\}$ \rightarrow D Example: Given $F =$

Using Closure to Infer ALL FDs

Step 1: Compute X⁺, for every set of attributes X:

 ${A}^+= {A}, {B}^+= {B,D}, {C}^+= {C}, {D}^+= {D}, {A,B}^+= {A,B,C,D},$ ${A, C}^+ = {A, C}$, ${A, D}^+ = {A, B, C, D}$, ${A, B, C}^+ = {A, B, D}^+ = {A, C, D}^+ =$ ${A,B,C,D}, {B,C,D}^+ = {B,C,D}, {A,B,C,D}^+ = {A,B,C,D}$

Step 2: Enumerate all FDs $X \rightarrow Y$, s.t. $Y \subset X^+$ and $X \cap Y = \emptyset$:

Example: Given $F =$

Using Closure to Infer ALL FDs

Step 1: Compute X⁺, for every set of attributes X:

 ${A}^+= {A}, {B}^+= {B,D}, {C}^+= {C}, {D}^+= {D}, {A,B}^+= {A,B,C,D},$ ${A, C}^+ = {A, C}$, ${A, D}^+ = {A, B, C, D}$, ${A, B, C}^+ = {A, B, D}^+ = {A, C, D}^+ =$ ${A,B,C,D}, {B,C,D}^+ = {B,C,D}, {A,B,C,D}^+ = {A,B,C,D}$

Y is in the closure of X

 ${A,B} \rightarrow C$

Example:

Given $F =$

 ${A, D} \rightarrow B$

 $\{B\}$ \rightarrow D

Step 2: Enumerate all FDs $X \rightarrow Y$, s.t. $Y \subseteq X^*$ and $X \cap Y = \emptyset$:

 $\{A,B\} \rightarrow \{C,D\}$, $\{A,D\} \rightarrow \{B,C\}$, $\{A,B,C\} \rightarrow \{D\}, \{A,B,D\} \rightarrow \{C\},$ ${A, C, D} \rightarrow {B}$

Why Do We Need the Closure?

With closure we can find keys and superkeys of a relation

For each set of attributes X

- 1. Compute X⁺
- 2. If $X^+=$ set of all attributes then X is a superkey
- 3. If X is minimal, then it is a key

Keys and Superkeys

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A superkey is a set of attributes A_1, \, ... , A_ns.t.
for any other attribute B in R,
we have \{A_1, ..., A_n\} \rightarrow B
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i.e. all attributes are functionally determined by a superkey

A key is a minimal superkey

This means that no subset of a key is also a superkey (i.e., dropping any attribute from the key makes it no longer a superkey)

Finding Keys and Superkeys

For each set of attributes X

- 1. Compute X⁺
- 2. If $X^+=$ set of all attributes then X is a superkey
- $3.$ If X is minimal, then it is a key

Example of Finding Keys

Product(name, price, category, color)

 ${name, category} \rightarrow price$ {category} → color

What is a key?

Example of Finding Keys

Product(name, price, category, color)

 ${name, category} \rightarrow price$ {category} → color

 $\{name, category\}^* = \{name, price, category\}$

- = the set of all attributes
- \Rightarrow this is a **superkey**

 \Rightarrow this is a **key**, since neither name nor category alone is a superkey

In-class Exercise

Given R(A, B, C, D) and FD's AB \rightarrow C, C \rightarrow D, D \rightarrow A

○ What are all keys of R?