CS 6400 A Final Review

Final Logistics

Final will be released Thursday Dec 4 at 3PM and due Friday Dec 5 at 9PM

- Open books and notes, closed Internet
- Unlimited time during the availability window. Submit finished exam on Gradescope

Clarification questions during exam

- Via private posts on Piazza
- Also check out the clarification question thread

The exam covers the entire class but will focus primarily on lectures not covered by the midterm. Contents EXCLUDED:

- lec 13: Multidimensional and Vector Indexes
- All lectures after lec 21 (Transaction Recovery)

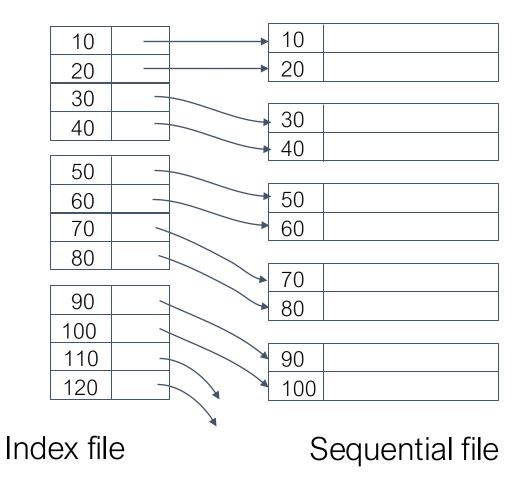
Past Exam: available on canvas, under Files->Past Exams

Index Basics

Dense index

A sequence of blocks holding keys of records and pointers to the

records

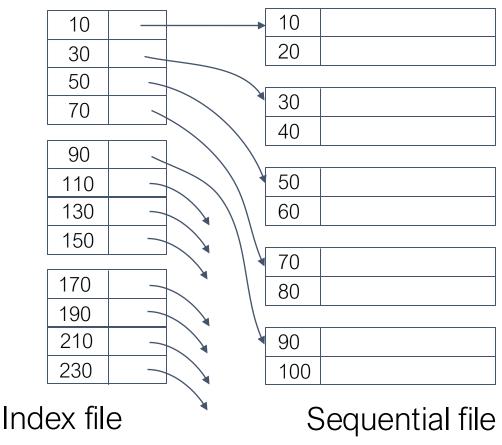


Sparse index

Has one key-pointer pair per block of the data file

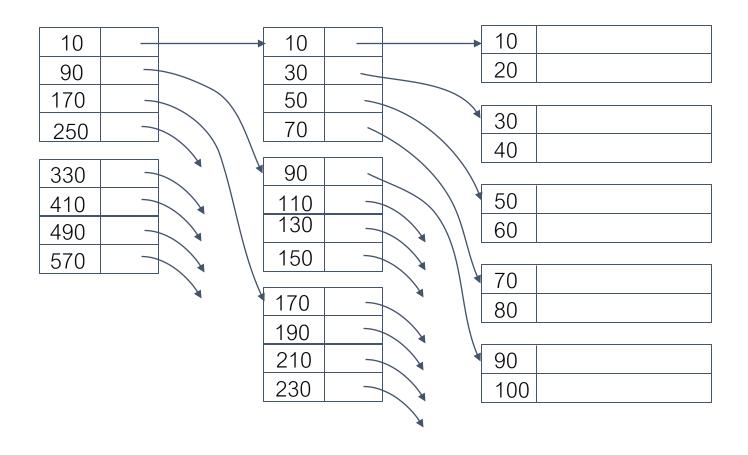
Uses less space than dense index, but needs more time to find a

record

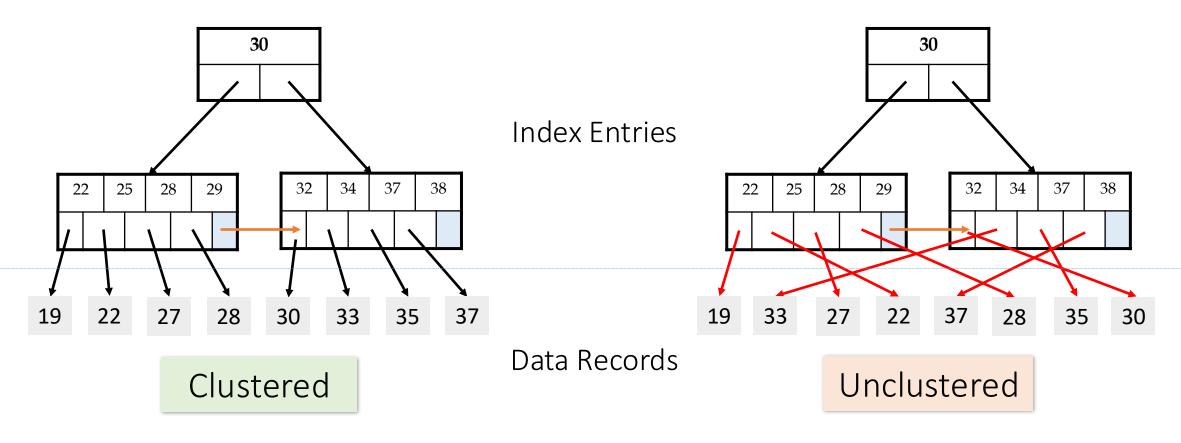


Multiple levels of index

If the index file is still large, add another level of indexing



Clustered vs. Unclustered Index



1 Random Access IO + Sequential IO (# of pages of answers)

Random Access IO for each value (i.e. # of tuples in answer)

Clustered can make a *huge* difference for range queries!

B+ Tree

B+ Tree Basics

Non-leaf or internal node $10 \quad 20 \quad 30$ k < 10 $20 \le k < 30$ $10 \le k < 20$ $22 \quad 25 \quad 28$

Parameter *d* = the degree

Each non-leaf ("interior") node has node has ≥ d and ≤ 2d keys*

The *k* keys in a node define *k*+1 ranges

*except for root node, which can have between **1** and 2d keys

For each range, in a *non-leaf* node, there is a **pointer** to another node with keys in that range

B+ Tree Basics

Age: 11

Age: 21

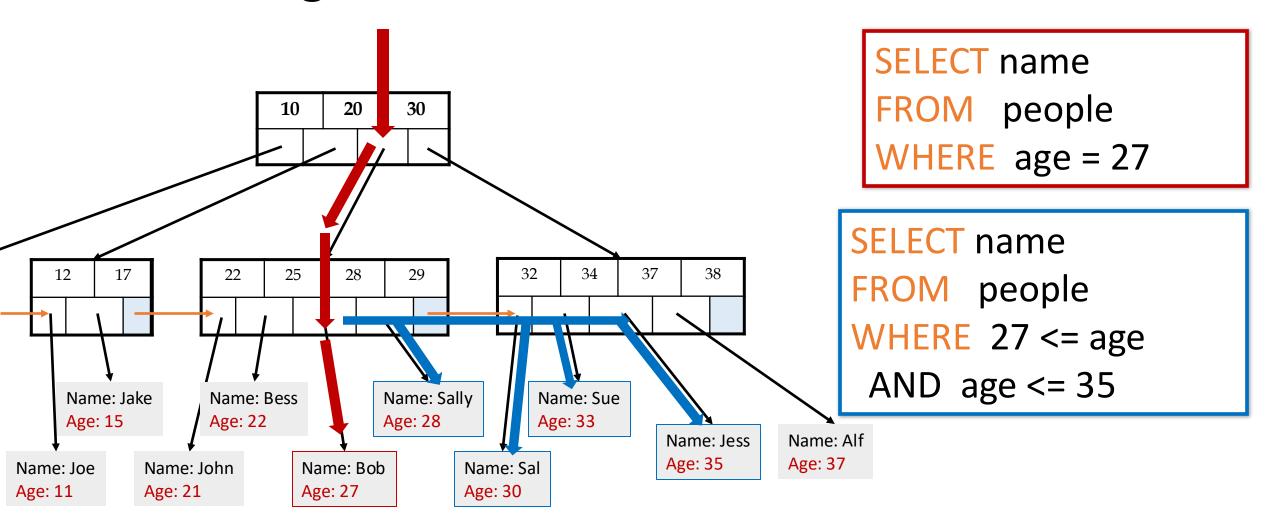
Age: 27

2d keys, and are different in that: Non-leaf or *internal* node 20 30 10 Their key slots contain pointers to data records Leaf nodes They contain a pointer to the next leaf node as well, 17 32 34 37 38 12 22 25 28 29 for faster sequential traversal Name: Jake Name: Sally Name: Bess Name: Sue Age: 15 Age: 22 Age: 28 Age: 33 Name: Jess Name: Alf Age: 35 Age: 37 Name: John Name: Bob Name: Sal Name: Joe

Age: 30

Leaf nodes also have between d and

Searching a B+ Tree



B+ Tree Cost Model

Note that exact search is just a special case of range search (R = 1)

Goal: Get the results set of a range (or exact) query with minimal IO

Key idea:

- A B+ Tree has high *fanout* (*d* ~= 10²-10³), which means it is very shallow → we can get to the right root node within a few steps!
- Then just traverse the leaf nodes using the horizontal pointers

Details:

- One node per page (thus page size determines d)
- Fill only some of each node's slots (the *fill-factor*) to leave room for insertions
- We can keep some levels of the B+ Tree in memory!

The <u>fanout</u> f is the number of pointers coming out of a node. Thus:

$$d+1 \le f \le 2d+1$$

Note that we will often approximate f as constant across nodes!

We define the <u>height</u> of the tree as counting the root node. Thus, given constant fanout **f**, a tree of height **h** can index **f**^h pages and has **f**^{h-1} leaf nodes

B+ Tree Cost Model

Given:	 Fill-factor <i>F</i> <i>B</i> available pages in buffer A B+ Tree over <i>N</i> pages f is the average fanout 	
Input:	A a range query.	
Output:	The R values that match	
IO COST:		Depth of the B+ Tree: For each level of the B+ Tree we read in one node = one page
	$ \left[\log_f \frac{N}{F} \right] - L_B + \mathbf{Cost}(Out) $ $ where B \ge \sum_{l=0}^{L_B-1} f^l $	# of levels we can fit in memory: These don't cost any IO!
		This equation is just saying that the sum of all the nodes for L_B levels must fit in buffer

Practice Question

- 4. Indexing Problem
 - 4.2
 - 4.3

Query Optimization

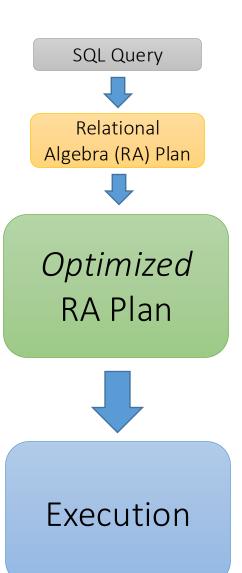
Logical vs. Physical Optimization

Logical optimization:

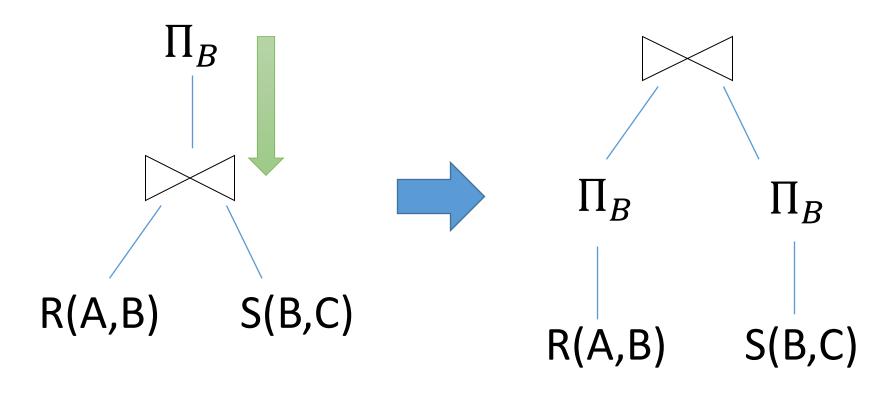
- Find equivalent plans that are more efficient
- Intuition: Minimize # of tuples at each step by changing the order of RA operators

Physical optimization:

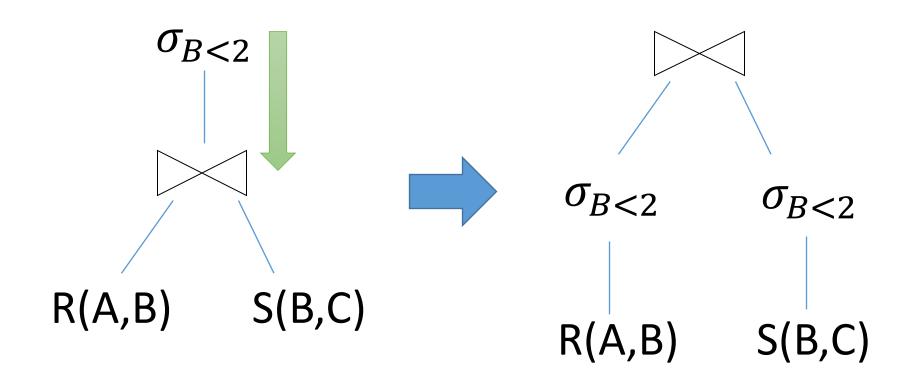
- Find algorithm with lowest IO cost to execute our plan
- Intuition: Calculate based on physical parameters (buffer size, etc.) and estimates of data size (histograms)



Logical Optimization: "Pushing down" projection



Logical Optimization: "Pushing down" selection



RA commutators

The basic commutators:

- Push projection through (1) selection, (2) join
- Push selection through (3) selection, (4) projection, (5) join
- Also: Joins can be re-ordered!

Note that this is not an exhaustive set of operations

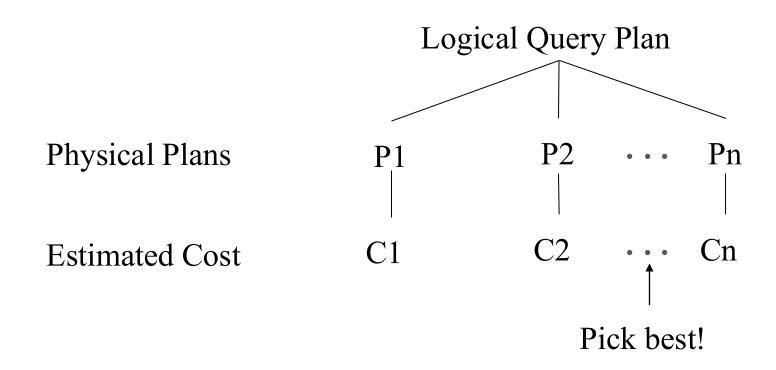
• This covers local re-writes; global re-writes possible but much harder

This simple set of tools allows us to greatly improve the execution time of queries by optimizing RA plans!

Practice Question

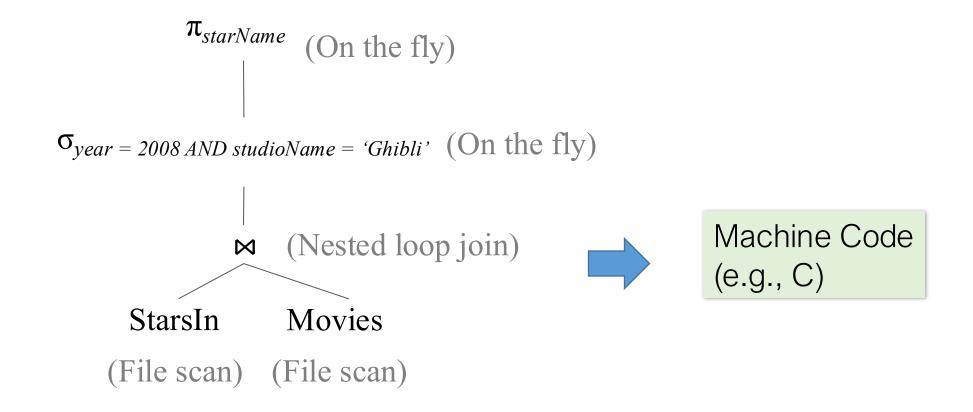
• 5.1 Logical Optimization

Select physical query plan



In general, there can be many possible physical plans

Query execution



The best physical plan is translated to actual machine code

Estimating the cost of a physical query plan

Step 1: Estimate the size of results

- Projection
- Selection
- Joins

Step 2: Estimate the # of disk I/O's

Estimating size of join

 $R(X,Y)\bowtie S(Y,Z)$

Two simplifying assumptions

- Containment of value sets: if $V(R,Y) \le V(S,Y)$, then every Y-value of R is a Y-value of S
- Preservation of value sets: $V(R \bowtie S, X) = V(R, X)$

Case 1:
$$V(R, Y) \ge V(S, Y)$$

 $\Rightarrow T(R \bowtie S) = T(R)T(S)/V(R, Y)$

Case 2:
$$V(R,Y) < V(S,Y)$$

$$\Rightarrow T(R \bowtie S) = T(R)T(S)/V(S,Y)$$

For each pair (r, s), we know that the Y-value of S is one of the Y-values of R by containment of value sets, so the probability of r having the same Y-value is 1/V(R,Y)

$$T(R \bowtie S) = T(R)T(S)/\max(V(R,Y),V(S,Y))$$

10 Cost Estimation via Histograms

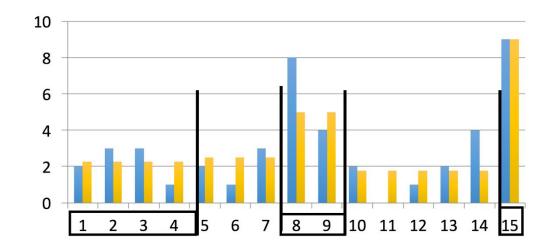
- For index selection:
 - What is the cost of an index lookup?
- Also for deciding which algorithm to use:
 - Ex: To execute $R \bowtie S$, which join algorithm should DBMS use?
 - What if we want to compute $\sigma_{A>10}(R)\bowtie\sigma_{B=1}(S)$?
- In general, we will need some way to estimate intermediate result set sizes

Histograms provide a way to efficiently store estimates of these quantities

Histogram types

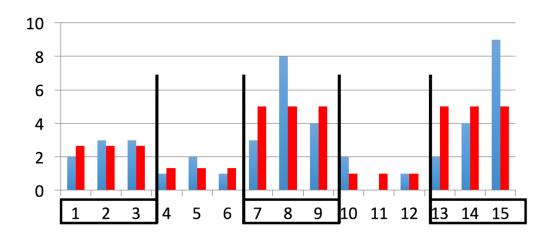
Equi-depth

All buckets contain roughly the same number of items (total frequency)



Equi-width

All buckets roughly the same width



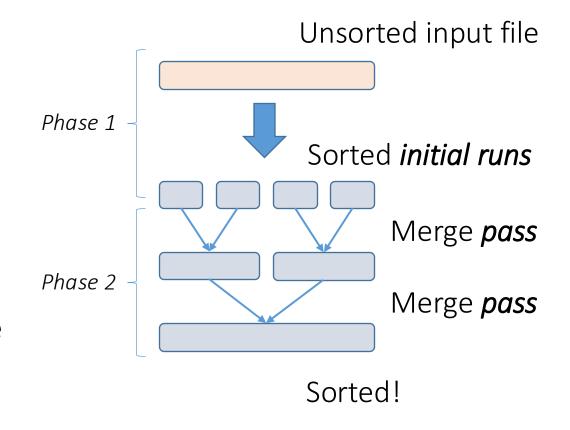
EMS and Join Algorithms

External Merge Sort Algorithm

 Goal: Sort a file that is much bigger than the buffer

• Key idea:

- Phase 1: Split file into smaller chunks ("initial runs") which can be sorted in memory
- Phase 2: Keep merging (do "passes") using external merge algorithm until one sorted file!



External Merge Algorithm

Goal: Merge sorted files that are much bigger than buffer

- Basic algorithm
 - (B+1)-length initial runs
 - B-way merging
- Repacking optimization for longer initial runs
 - Effect: runs will have ~2(B+1) length

$$2N(\lceil \log_2 N \rceil + 1) \longrightarrow 2N(\left\lceil \log_2 \frac{N}{B+1} \right\rceil + 1) \longrightarrow 2N(\left\lceil \log_B \frac{N}{B+1} \right\rceil + 1)$$

Starting with runs of length 1

Starting with runs of length *B+1*

Performing **B**-way merges

External Merge Sort Algorithm

Given:	B+1 buffer pages	
Input:	Unsorted file of length N pages	
Output:	The sorted file	
IO COST:	$2N(\left\lceil \log_{B} \left\lceil \frac{N}{B+1} \right\rceil \right\rceil + 1)$	Phase 1: Initial runs of length B+1 are created • There are $\left\lceil \frac{N}{B+1} \right\rceil$ of these • The IO cost is 2N Phase 2: We do passes of B-way merge until fully merged • Need $\left\lceil \log_B \left\lceil \frac{N}{B+1} \right\rceil \right\rceil$ passes • The IO cost is 2N per pass

Join Algorithms: Overview

For $R \bowtie S$ on A

- NLJ: An example of a *non-*IO aware join algorithm
- BNLJ: Big gains just by being IO aware & reading in chunks of pages!

Quadratic in P(R), P(S)I.e. O(P(R)*P(S))

- SMJ: Sort R and S, then scan over to join!
- HJ: Partition R and S into buckets using a hash function, then join the (much smaller) matching buckets

Given sufficient buffer space, **linear** in P(R), P(S) I.e. $\sim O(P(R)+P(S))$

By only supporting equijoins & taking advantage of this structure!

Nested Loop Join (NLJ)

```
Compute R \bowtie S \ on \ A:
```

for r in R:

for s in S:

if
$$r[A] == s[A]$$
:

yield (r,s)

Note that IO cost based on number of pages loaded, not number of tuples!

Cost:

$$P(R) + T(R)*P(S) + OUT$$

- 1. Loop over the tuples in R
- 2. For every tuple in R, loop over all the tuples in S
- 3. Check against join conditions
- 4. Write out (to page, then when page full, to disk)

Have to read *all of S* from disk for *every tuple in R!*

Block Nested Loop Join (BNLJ)

Given **B+1** pages of memory

```
Compute R \bowtie S \ on \ A:
 for each B-1 pages pr of R:
  for page ps of S:
   for each tuple r in pr:
     for each tuple s in ps:
      if r[A] == s[A]:
       yield (r,s)
```

Again, *OUT* could be bigger than P(R)*P(S)... but usually not that bad

Cost:

$$P(R) + \frac{P(R)}{B-1}P(S) + OUT$$

- 1. Load in B-1 pages of R at a time (leaving 1 page each free for S & output)
- 2. For each (B-1)-page segment of R, load each page of S
- 3. Check against the join conditions

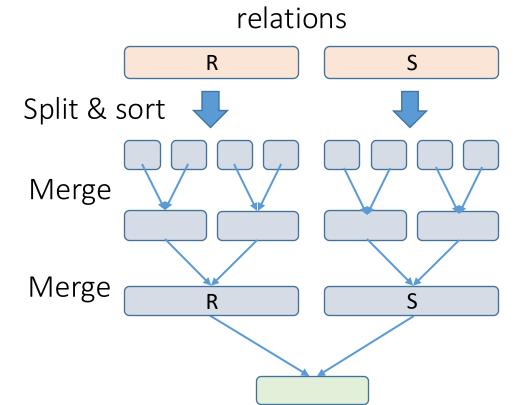
4. Write out

Basic SMJ: Total cost

Cost of SMJ is cost of sorting R and S...

Plus the **cost of scanning**: $^{\sim}P(R)+P(S)$

 Because of backup: in worst case P(R)*P(S); but this would be very unlikely



Unsorted input

Plus the cost of writing out

$$\sim$$
 Sort(P(R)) + Sort(P(S))
+ P(R) + P(S) + OUT

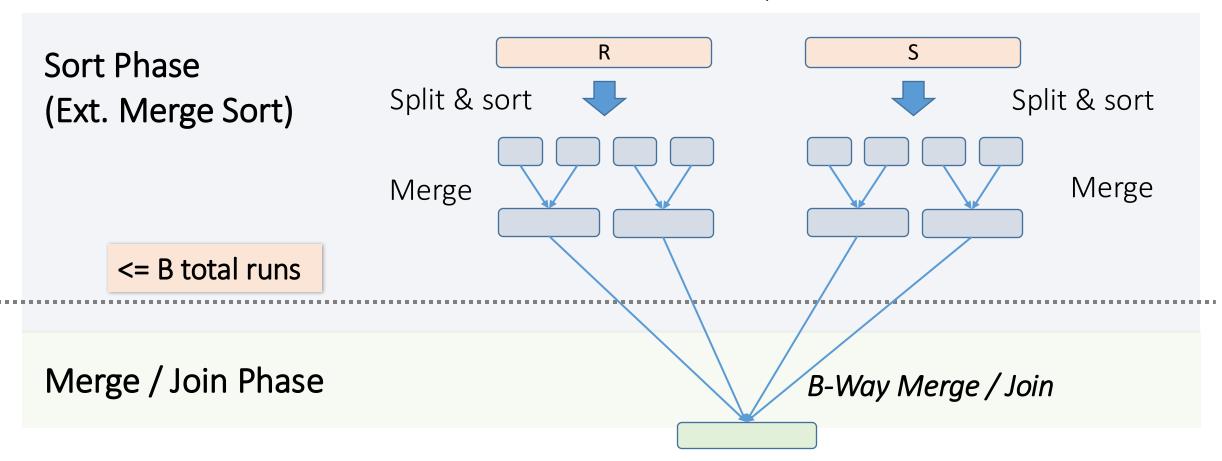
Recall: Sort(N)
$$\approx 2N \left(\left[\log_B \frac{N}{B+1} \right] + 1 \right)$$

Note: this is WITHOUT the repacking

optimization

SMJ Optimization

Unsorted input relations



Optimization: Keep merging until (# of runs of R) + (# of runs of S) $\leq B$, then we are ready to complete the join in one pass

Hash Join: High-level procedure

Given *B+1* buffer pages

To compute $R \bowtie S \ on \ A$:

- 1. Partition Phase: Using one (shared) hash function h_B per pass partition R and S into **B** buckets.
 - Each phase creates B more buckets that are a factor of B smaller.
 - Repeatedly partition with a new hash function
 - Stop when all buckets for one relation are smaller than B-1 pages

Each pass takes 2(P(R) + P(S))

- 2. Join Phase: Take pairs of buckets whose tuples have the same values for *h*, and join these
 - Use BNLJ here for each matching pair.

$$P(R) + P(S) + OUT$$

Join phase cost can be worse due to hash collision and skew

SMJ vs. HJ

Given enough memory, both SMJ and HJ have performance:

$$\sim$$
3(P(R)+P(S)) + OUT

"Enough" memory =

- SMJ: $B^2 > max\{P(R), P(S)\}$
- HJ: $B^2 > min\{P(R), P(S)\}$

Hash Join superior if relation sizes differ greatly.

Practice Question

• 6. Query Optimization

Transaction

Transactions: Basic Definition

A <u>transaction</u> ("TXN") is a sequence of one or more *operations* (reads or writes) which reflects *a single real-world transition*.

In the real world, a TXN either happened completely or not at all

```
START TRANSACTION

UPDATE Product

SET Price = Price - 1.99

WHERE pname = 'Gizmo'

COMMIT
```

Motivation for Transactions

Grouping user actions (reads & writes) into *transactions* helps with two goals:

 Recovery & Durability: Keeping the DBMS data consistent and durable in the face of crashes, aborts, system shutdowns, etc.

2. <u>Concurrency:</u> Achieving better performance by parallelizing TXNs *without* creating anomalies

Transaction Properties: ACID

- Atomic
 - State shows either all the effects of txn, or none of them
- Consistent
 - Txn moves from a state where integrity holds, to another where integrity holds
- Isolated
 - Effect of txns is the same as txns running one after another (ie looks like batch mode)
- Durable
 - Once a txn has committed, its effects remain in the database

ACID continues to be a source of great debate!

Comparison of SQL isolation levels

Isolation Level	Dirty Reads	Nonrepeatable Reads	Phantoms
READ UNCOMMITTED	✓	✓	✓
READ COMMITTED	O	✓	✓
REPEATABLE READ	0	O	✓
SERIALIZABLE	O	O	O

Why Interleave TXNs?

Interleaving TXNs might lead to anomalous outcomes... why do it?

- Several important reasons:
 - Individual TXNs might be slow- don't want to block other users during!
 - Disk access may be slow- let some TXNs use CPUs while others accessing disk!

All concern large differences in *performance*

Scheduling Definitions

 A <u>serial schedule</u> is one that does not interleave the actions of different transactions

• A and B are <u>equivalent schedules</u> if, *for any database state*, the effect on DB of executing A **is identical to** the effect of executing B

A <u>serializable schedule</u> is a schedule that is equivalent to *some* serial execution of the transactions.

The word "some" makes this definition powerful & tricky!

Conflicts: Anomalies with Interleaved Execution

Conditions for conflicts:

- The operations must belong to different transactions (no conflict within the same transaction).
- The operations must access the same database object
- At least one of the operations must be a write operation.

Types of conflicts:

- Write-Read (WR)
- Read-Write (RW)
- Write-Write (WW)

DB isolation levels define which types of conflicts a database will prevent or allow.

<u>Implication for schedules:</u>

A pair of consecutive actions that cannot be interchanged without changing behavior

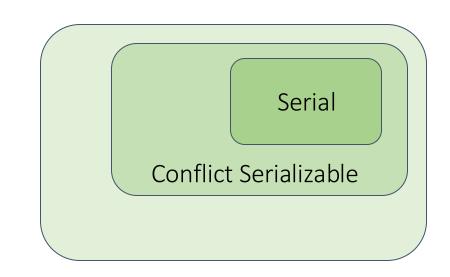
Characterizing Schedules based on Serializability (2)

Conflict equivalent

- Two conflict equivalent schedules have the same effect on a database
- All pairs of conflicting actions are in same order
- one schedule can be obtained from the other by swapping "non-conflicting" actions
 - either on two different objects
 - or both are read on the same object

Conflict serializable

• A schedule S is said to be conflict serializable if it is conflict equivalent to some serial schedule S'.



Testing for conflict serializability

Through a precedence graph:

- Looks at only read_Item (X) and write_Item (X) operations
- Constructs a precedence graph (serialization graph) a graph with directed edges
- An edge is created from Ti to Tj if one of the operations in Ti appears before a conflicting operation in Tj
- The schedule is serializable if and only if the precedence graph <u>has</u> no cycles.

Practice Question

- 1. Serializability
 - 1.1 Conflicts and Serializability
 - 1.2 Conflict Serializable

Two-phase locking (2PL)

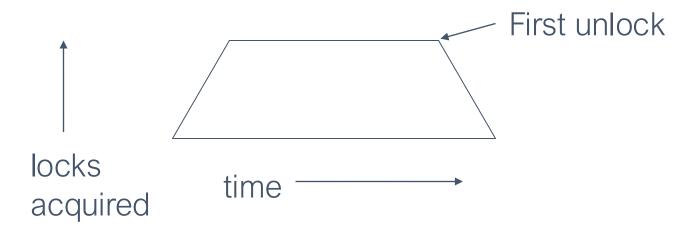
TXNs obtain:

- An X (exclusive) lock on object before writing.
 - If a TXN holds, no other TXN can get a lock (S or X) on that object.

- An S (shared) lock on object before reading
 - If a TXN holds, no other TXN can get an X lock on that object

Two-phase locking (2PL)

- In every transaction, all lock actions precede all unlock actions
- Guarantees a legal schedule of consistent transactions is conflict serializable



Practice Question

• 2.1. 2PL Feasibility

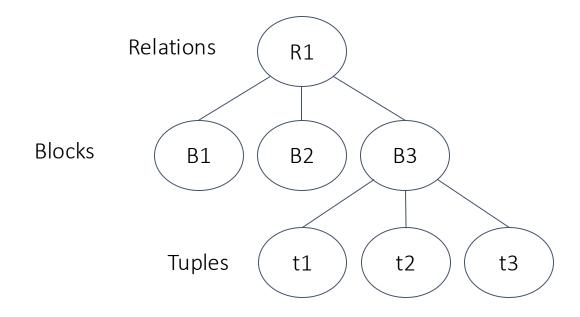
Locking with several modes

Compatibility matrix

		Lock requested		
		S	X	
Lock held in mode	S X	Yes No	No No	

Locking with Multiple Granularities

- Ordinary locks: S and X
- Warning locks: I (shows intention to lock)



Compatibility matrix

• For shared, exclusive, and intention locks

Requestor

		IS	IX	S	X
Holder	IS IX S X	Yes Yes	Yes No	Yes No Yes No	No No

Practice Question

• 2.3 Locking with multiple granularities

Optimistic Concurrency Control

Optimistic methods

- Two methods: validation (covered next), and timestamping
- Assume no unserializable behavior
- Abort transactions when violation is apparent
- may cause transactions to rollback

In comparison, locking methods are pessimistic

- Assume things will go wrong
- Prevent nonserializable behavior
- Delays transactions but avoids rollbacks

Optimistic approaches are often better than lock when transactions have low interference (e.g., read-only)

To validate, scheduler maintains three sets

START: set of transactions that started, but have not validated

START(T), the time at which T started

VAL: set of transactions that validated, but not yet finished write phase

 VAL(T), time at which T is imagined to execute in the hypothetical serial order of execution

FIN: set of transactions that have completed write phase

 $_{\circ}$ FIN(T), the time at which T finished.

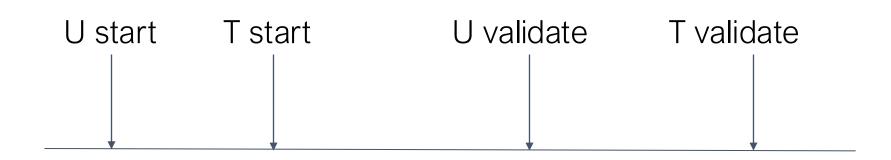
Validation rules (assume U validated)

Rule 1: if FIN(U) > START(T), $RS(T) \cap WS(U) = \emptyset$

$$WS(U) = \{A, B\}$$

$$RS(T) = \{B, C\}$$

This violates rule 1 because T may be reading B before U writes B



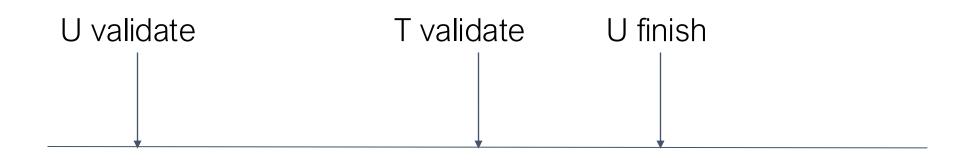
Validation rules (assume U validated)

Rule 2: if FIN(U) > VAL(T), $WS(T) \cap WS(U) = \emptyset$

$$WS(U) = \{A, B\}$$

$$WS(T) = \{B, C\}$$

This violates rule 2 because T may write B before U writes B



Practice Question

• 2.2 Optimistic Concurrency Control

Basic Idea: (Physical) Logging

- Record UNDO information for every update!
 - Sequential writes to log
 - Minimal info (diff) written to log

- The log consists of an ordered list of actions
 - Log record contains:

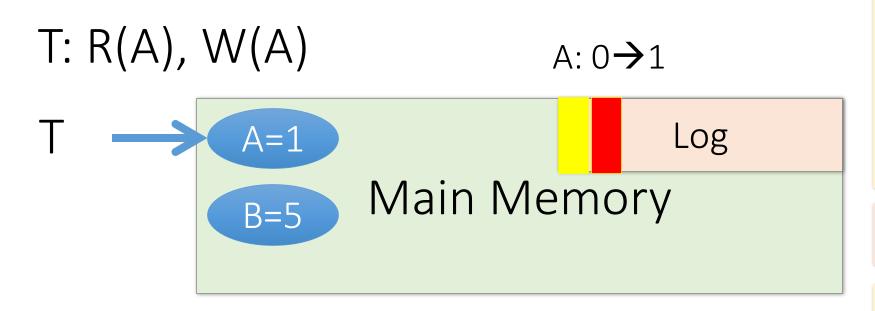
 $\langle T, X, v, w \rangle$: T changed value of X from v to w

Why do we need logging for atomicity?

- Couldn't we just write TXN to disk **only** once whole TXN complete?
 - Then, if abort / crash and TXN not complete, it has no effect- atomicity!
 - With unlimited memory and time, this could work...
- However, we need to log partial results of TXNs because of:
 - Memory constraints (enough space for full TXN??)
 - Time constraints (what if one TXN takes very long?)

We need to write partial results to disk! ...And so we need a **log** to be able to *undo* these partial results!

Write-ahead Logging (WAL) Commit Protocol



This time, let's try committing <u>after we've</u> written log to disk but before we've written data to disk... this is WAL!

OK, Commit!

If we crash now, is T durable?

A=0 Data on Disk

Log on Disk

Write-ahead Logging (WAL) Commit Protocol

T: R(A), W(A)

T

Main Memory

A=1
Data on Disk

A: 0 > 1



This time, let's try committing <u>after we've</u> written log to disk but before we've written data to disk... this is WAL!

OK, Commit!

If we crash now, is T durable?

USE THE LOG!

Write-Ahead Logging (WAL)

• DB uses Write-Ahead Logging (WAL) Protocol:

Each **update** is logged! Why not reads?

1. Must *force log record* for an update *before* the corresponding data page goes to storage

→ <u>Atomicity</u>

- 2. Must write all log records for a TX before commit
- → <u>Durability</u>

Undo logging

Idea: Undo incomplete transactions, and ignore committed ones

		Memory			sk	
Action	t	Α	В	A	В	Log
						<start <i="">T></start>
READ(A, t)	8	8		8	8	
t := t * 2	16	8		8	8	
WRITE(A, t)	16	16		8	8	<t, 8="" a,=""></t,>
READ(B, t)	8	16	8	8	8	
t := t * 2	16	16	8	8	8	
WRITE(B, t)	16	16	16	8	8	<t, 8="" b,=""></t,>
FLUSH LOG						
OUTPUT(A)	16	16	16	16	8	
OUTPUT(B)	16	16	16	16	16	
FLUSH LOG						<commit t=""></commit>

Undo log format:

 $\langle T, X, \underline{v} \rangle$: T updated database element X whose old value is \underline{v}

Recovery using undo logging

Simplifying assumption: use entire log, no matter how long

	Memory Di			Disk		
Action	t	Α	В	Α	В	Log
						<start t=""></start>
READ(A, t)	8	8		8	8	
t := t * 2	16	8		8	8	
WRITE(A, t)	16	16		8	8	<t, 8="" a,=""></t,>
READ(B, t)	8	16	8	8	8	
t := t * 2	16	16	8	8	8	
WRITE(B, t)	16	16	16	8	8	<t, 8="" b,=""></t,>
FLUSH LOG						
OUTPUT(A)	16	16	16	16	8	
OUTPUT(B)	16	16	16	16	16	
						<commit t=""></commit>
FLUSH LOG						

Recovery

A = 16 B = 16

Ignore (*T* was committed)



Ignore (*T* was committed)



Observe < COMMIT T> record

Crash

Nonquiescent checkpointing

- Motivation: avoid shutting down system while checkpointing
- Checkpoint all active transactions, but allow new transactions to enter system

```
<START T1>
<T1, A, 5>
<START T2>
<T2, B, 10>
<START CKPT (T1, T2)>
<T2, C, 15>
<START T3>
<T1, D, 20>
<COMMIT T1>
<T3, E, 25>
<COMMIT T2>
<END CKPT>
<T3, F, 30>
```

Nonquiescent checkpointing

Motivation: avoid shutting down system while checkpointing

Checkpoint all active transactions, but allow new transactions

to enter system

```
<START T1>
<T1, A, 5>
<START T2>
<T2, B, 10>
<START CKPT (T1, T2)>
<T2, C, 15>
<START T3>
<T1, D, 20>
<COMMITT1>
<T3, E, 25>
<COMMIT T2>
<END CKPT>
<T3, F, 30>
```

If we first meet <END CKPT>, only need to recover until <START CKPT (T1, T2)>

Nonquiescent checkpointing

Motivation: avoid shutting down system while checkpointing

Checkpoint all active transactions, but allow new transactions to

enter system

```
<START T1>
<T1, A, 5>
<START T2>
<T2, B, 10>
<START CKPT (T1, T2)>
<T2, C, 15>
<START T3>
<T1, D, 20>
                   Crash
<COMMITT1>
<T3, E, 25>
<COMMIT T2>
<END CKPT>
<T3, F, 30>
```

If we first meet <START CKPT (T1, T2)>, only need to recover until <START T1>

Redo logging

Redo logging ignores incomplete transactions and repeats committed ones

Undo logging cancels incomplete transactions and ignores committed ones

 $< T, X, \underline{\lor} > \text{ now means } T \text{ wrote } \underline{\text{new}} \text{ value } v \text{ for database element } X$

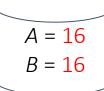
One rule: all log records (e.g., < T, X, v > and < COMMIT T >) must appear on disk before modifying any database element X on disk

Recovery with redo logging

Scan log forward and redo committed transactions

Memory Disk									
Action	t	Α	В	Α	В	Log			
						<start t=""></start>			
READ(A, t)	8	8		8	8				
t := t * 2	16	8		8	8				
WRITE(A, t)	16	16		8	8	<t, 16="" a,=""></t,>			
READ(B, t)	8	16	8	8	8				
t := t * 2	16	16	8	8	8				
WRITE(B, t)	16	16	16	8	8	<t, 16="" b,=""></t,>			
						<commit t=""></commit>			
FLUSH LOG							—— Crash		
OUTPUT(A)	16	16	16	16	8		Crasii		
OUTPUT(B)	16	16	16	16	16				

Recovery



Nonquiescent checkpointing for redo log

Write to disk all DB elements modified by committed transactions

```
<START T1>
<T1, A, 5>
<START T2>
<COMMIT T1>
<T2, B, 10>
<START CKPT (T2)>
<T2, C, 15>

Write to disk all DB elements by transactions
<START T3>
that already committed when START CKPT was
<T3, D, 20>
written to log (i.e., T1)
<END CKPT>
<COMMIT T2>
<COMMIT T3>
```

Nonquiescent checkpointing for redo log

 After crash, redo committed transactions that either started after START CKPT or were active during START CKPT

```
<T1, A, 5>
<START T2>
<COMMIT T1>
<T2, B, 10>
<START CKPT (T2)>
<T2, C, 15>
<START T3>
<T3, D, 20>
<END CKPT>
<COMMIT T2>
<COMMIT T3>

Crash
```

Undo/redo logging

More flexible than undo or redo logging in ordering actions

< T, X, v, w > : T changed value of X from v to w

One rule: <T, X, v, w> must appear on disk before modifying X on disk

Nonquiescent checkpointing for undo/redo logging

Simpler than other logging methods

```
<T1, A, 4, 5>
<T1, A, 4, 5>
<START T2>
<COMMIT T1>
<T2, B, 9, 10>
<START CKPT (T2)>
<T2, C, 14, 15>
<START T3>
<T3, D, 19, 20>
<END CKPT>
```

Write to disk all the buffers that are dirty

Nonquiescent checkpointing for undo/redo logging

After a crash, redo committed transactions, and undo uncommitted ones

```
<T1, A, 4, 5>
<T1, A, 4, 5>
<START T2>
<COMMIT T1>
<T2, B, 9, 10>
<START CKPT (T2)>
<T2, C, 14, 15>
<T2, C, 14, 15>
<START T3>
<T3, D, 19, 20>
<END CKPT>
<COMMIT T2>
<COMMIT T2>
<COMMIT T3>
```

Redo T2 by setting C to 15 on disk (No need to set B to 10 thanks to CKPT) Undo T3 by setting D to 19 on disk

Practice Question

• 3. Recovery